

*Discussion of:*  
**Dissecting Factors**  
*by:*  
*Joseph Gerakos and Juhani Linnainmaa*

Kent Daniel<sup>†</sup>

<sup>†</sup>Columbia University, Graduate School of Business

2014 AFA Meeting  
4 January, 2014

# Outline

- Review of key findings
- Interpretation of findings:
  - “Beating” the FF 3-factor model.
  - What is  $dme_t$ ?
  - Mutual Fund Results.
- Conclusions

# GL fundamental-to-price measure decomposition

- 1 GL motivate their calculation of the “priced” book-to-price factor using a book-to-market ratio decomposition used in Daniel and Titman (2006, DT), and elsewhere:

$$bm_t \equiv \log \left( \frac{BE_t}{ME_t} \right) = bm_{t-\tau} + \log \left( \frac{BE_t}{BE_{t-\tau}} \right) - \log \left( \frac{ME_t}{ME_{t-\tau}} \right)$$

- 2 The three components are:
  - The log-BM ratio  $\tau$  periods ago:  $bm_{t-\tau}$ ,
  - The log-change in book-value:  $\log (BE_t/BE_{t-\tau})$ ,
  - The log-change in the firm size:  $\log (ME_t/ME_{t-\tau})$ .

# GL fundamental-to-price measure decomposition

- 1 One can further break down the changes in log BE and ME into the sum of each years' changes:

$$\begin{aligned}
 bm_t \equiv \log \left( \frac{BE_t}{ME_t} \right) &= \underbrace{bm_{t-\tau} + \log \left( \frac{BE_t}{BE_{t-\tau}} \right)}_{\sum_{s=0}^{\tau-1} dbe_{t-s}} - \underbrace{\log \left( \frac{ME_t}{ME_{t-\tau}} \right)}_{\sum_{s=0}^{\tau-1} dme_{t-s}} \\
 &= \sum_{s=0}^{\tau-1} dbe_{t-s} - \sum_{s=0}^{\tau-1} dme_{t-s}
 \end{aligned}$$

- 2 GL argue that  $bm_t$  will only be an optimal forecast of the cross-section of returns if, in projecting future returns onto the 3 components, the projection coefficients are equal.
- However, it is possible that the “components” of book-to-market forecast future returns differently
  - This would mean that B/M could be improved by re-weighting the different components.

# Beating size and book-to-market – Table 2

## Fama-MacBeth Regressions of returns on ...

Regressor	Model									
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)	(10)
$r_t^{1,1}$	-5.91 (-14.88)	-6.01 (-15.30)	-6.12 (-15.73)	-6.18 (-15.94)	-6.24 (-16.09)	-6.27 (-16.22)	-6.39 (-16.65)	-6.17 (-16.08)	-6.10 (-16.02)	-5.77 (-14.68)
$r_t^{2,12}$	0.64 (3.62)	0.64 (3.72)	0.62 (3.57)	0.61 (3.54)	0.58 (3.40)	0.57 (3.35)	0.54 (3.20)	0.65 (3.87)	0.68 (4.04)	0.74 (4.26)
$me_t$	-0.10 (-2.84)	-0.10 (-2.83)	-0.10 (-2.77)	-0.09 (-2.78)	-0.09 (-2.75)	-0.09 (-2.69)	-0.08 (-2.37)	-0.05 (-1.70)	-0.02 (-0.58)	
$bm_t$	0.27 (4.56)	0.19 (3.25)	0.14 (2.36)	0.11 (1.94)	0.10 (1.64)	0.07 (1.25)	0.07 (1.23)	0.07 (1.27)	0.08 (1.40)	
$dme_t$		0.24 (2.58)	0.27 (2.74)	0.30 (3.06)	0.32 (3.27)	0.33 (3.39)	0.36 (3.64)	-0.25 (-2.68)	-0.23 (-2.43)	-0.28 (-2.93)
$dme_{t-1}$			0.25 (3.04)	0.25 (3.03)	0.28 (3.30)	0.31 (3.58)	0.33 (3.90)	-0.22 (-2.64)	-0.20 (-2.40)	-0.24 (-2.80)
$dme_{t-2}$				0.25 (3.87)	0.27 (4.02)	0.29 (4.39)	0.29 (4.34)	-0.21 (-3.24)	-0.19 (-3.02)	-0.24 (-3.12)
$dme_{t-3}$					0.24 (3.80)	0.25 (3.94)	0.26 (4.02)	-0.18 (-2.86)	-0.17 (-2.75)	-0.24 (-3.36)
$dme_{t-4}$						0.21 (3.83)	0.23 (4.20)	-0.13 (-2.50)	-0.12 (-2.22)	-0.17 (-2.68)
Older $dmes$							Yes			
rank $chg_t$								-0.30 (-6.61)	-0.34 (-6.37)	-0.37 (-5.77)
rank $chg_t^2$									0.20 (6.55)	0.23 (6.47)

## Key Findings

- For forecasting future returns, GL improve on book-to-market (and size)
  - They are a “reweighted” BM ratio –  $\widehat{bm}_t$  – “beats”  $bm_t$  in Fama-MacBeth regressions, and in sorted portfolio tests.
    - $\widehat{bm}_t$  is a projection of  $bm_t$  on the last 4 years of  $dme_{t-s}$ , their size rank change variable, and  $\text{rank chg}_t^2$

$$\widehat{bm}_t = \sum_{s=0}^4 \hat{\gamma}_s dme_{t-s} + \hat{\gamma}_5 \cdot \text{rank chg}_t + \hat{\gamma}_6 \cdot \text{rank chg}_t^2$$

where the coefficients  $\hat{\gamma}_i$  are from the FM return forecasting regressions.

- $\widehat{me}_t$  is calculated using the same regressors.

## Key Findings (2)

- GL find that these “fixed”  $\hat{b}m_t$  and  $\hat{m}e_t$  factors better explain size and value sorted portfolios.
- They “explain” the profitability anomaly of Novy-Marx (2012)
- With the “fixed” FF3 benchmark, there is evidence that a substantial fraction of mutual-funds outperform, *net of fees*

# Is the MVE portfolio in span of Mkt, HML & SMB?

- Below are the realized Sharpe-ratios of the *ex-post* tangency portfolios based on trading in:
  - The three Fama and French (1993) portfolios (Mkt, SMB, HML)
  - Carhart (1997) price momentum portfolio UMD.
  - Daniel-Titman (2006a) issuance (ISU) and accrual (ACR) portfolios
    - All strategies are value-weighted and rebalanced annually.*

Mkt	Portfolio Weights (%)					ACR	Ex-Post Sharpe ratio
	SMB	HML	UMD	ISU			
100.00	—	—	—	—	—	—	0.31
75.07	24.93	—	—	—	—	—	0.32
28.19	14.63	57.18	—	—	—	—	0.80
21.13	10.16	41.92	26.79	—	—	—	1.18
18.82	15.33	13.87	9.55	42.44	—	—	1.55
17.35	14.47	12.32	8.18	36.65	11.04	—	1.60



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## The BM decomposition is Arbitrary

- 1 GL motivate their calculation of the book-return using a book-to-market ratio decomposition:

$$bm_{i,t} \equiv \log \left( \frac{BE_{i,t}}{ME_{i,t}} \right) = bm_{i,t-\tau} + \log \left( \frac{BE_{i,t}}{BE_{i,t-\tau}} \right) - \log \left( \frac{ME_{i,t}}{ME_{i,t-\tau}} \right)$$

- 2 However, this decomposition is arbitrary. We could also use book- and market-value per share:

$$bm_{i,t} = bm_{i,t-\tau} + \log \left( \frac{B_{i,t}}{B_{i,t-\tau}} \right) - \log \left( \frac{P_{i,t}}{P_{i,t-\tau}} \right)$$

- 3 and, for that matter, we can add any constant  $n_{i,t}$  to both the changes in book and market:

$$bm_{i,t} = bm_{i,t-\tau} + \left[ \log \left( \frac{BE_{i,t}}{BE_{i,t-\tau}} \right) + n_{i,t} \right] - \left[ \log \left( \frac{ME_{i,t}}{ME_{i,t-\tau}} \right) + n_{i,t} \right]$$

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## Why dme?

- Intuitively,  $\hat{b}m_t$  (and  $\hat{m}e_t$ ) probably better “explain” different sets of portfolio returns because they come closer to spanning the MVE portfolios.
- This begs the question of why  $\hat{b}m_t$  should be better than  $bm$ .

## Why $dme$ ?

- One would think that  $dme_t$  would be a lot like log returns.
  - It isn't.
- the difference between  $dme$  and log returns  $r_{i,t}$  is share issuance (Daniel and Titman 2006):

$$\sum_{s=0}^{\tau-1} dme_{i,t-s} = r_i(t - \tau, t) + \iota_i(t - \tau, t)$$



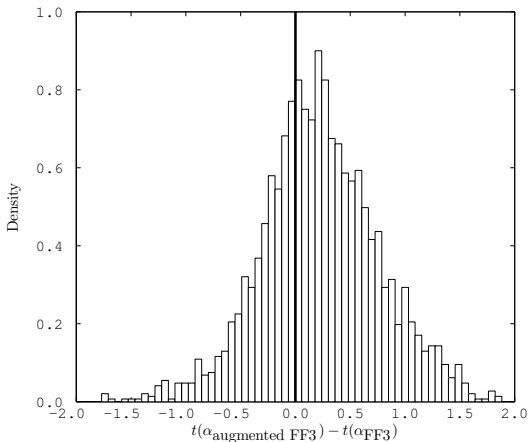
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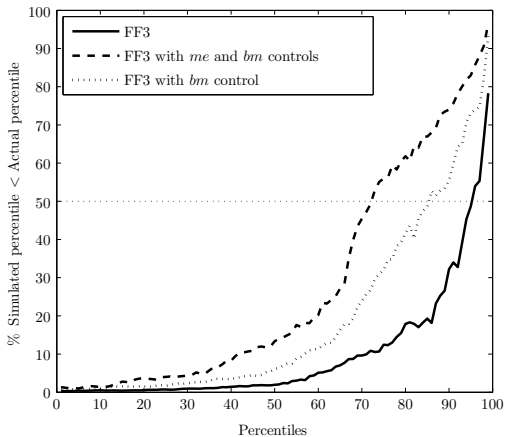
$$\sum_{s=0}^{\tau-1} dme_{i,t-s} = r_i(t - \tau, t) + \nu_i(t - \tau, t)$$

# Fig 1 – Histogram of differences in fund $t(\alpha)$ s

Raw FF3 factor model vs. “fixed” FF3 factor model.



## Figure 2 – Luck vs. Skill



# Mutual Fund Performance

- Figure 1 suggest that the post-expense  $\alpha$ s of *the average* fund increase when the “fixed” factor model is used.
- This seems odd, as Fama and French (2010) show that the time series of returns for average fund is very, very close to the market minus fees/expenses.
  - This seems like it has to imply the the average fund’s loading on any factor other than the market must be very close to zero
  - Thus, the average alpha shouldn’t be affected by an improvement of the efficiency of the factors.
- This is perhaps worth digging into a bit more.

# Conclusions

- It is reasonable that constructing a set of factors that come closer to spanning the MVE portfolio will better explain individual asset and portfolio returns.
- If the only goal is increasing the Sharpe-Ratio of the “factor,” you can almost certainly do better than just linear combinations of  $dme_{t-s}$ .
  - Clearly, given complete freedom in the specification of the decomposition, you can really “improve” on the simple book-to-price ratio.
- However, the end goal of this line of research is to understand the economic mechanisms that cause these premia to arise.

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